

SAXON Homeschool

Middle Grades Sampler

Math 5/4, Math 6/5, Math 7/6, Math 8/7, and Algebra 1/2

Math 5/4, Math 6/5, Math 7/6, Math 8/7, and *Algebra ¹/₂* form a series of courses to move students from primary grades to algebra. Each course contains a series of daily lessons covering all areas of general math. Each lesson presents a small portion of math content (called an increment) that builds on prior knowledge and understanding.

Students are not required or expected to grasp a concept fully the first time it is presented. After an increment is introduced, it becomes a part of the student's daily work for the rest of the year. Students will have many opportunities to gain understanding and to achieve mastery. This cumulative, continual practice ensures that students will retain what they have learned.

This sampler includes materials that are representative of the Saxon math program, including samples of Lessons and Investigations.

We hope these materials will assist you in your evaluation of the Saxon program.

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Math 8/7, Lesson 35 Sample taken from Math 8/7 (Third Edition), page 235



Sample taken from Math 8/7 (Third Edition), page 236

236 Saxon Math 8/7-Homeschool Example 2 Add: 0.1 + 0.2 + 0.3 + 0.4 Solution We align the decimal points vertically 0.1and add. The sum is 1.0, not 0.10. 0.2Since 1.0 equals 1, we can simplify the 0.3 answer to 1. + 0.41.0 = 1Example 3 Subtract: 12.3 - 4.567 Solution We write the first number above the second number, aligning the decimal points. We write zeros in the empty 4.567places and subtract. 7.733 Example 4 Subtract: 5 - 4.32 Solution We write the whole number 5 with a 5.00 decimal point and write zeros in the 4.32two empty decimal places. Then we 0.68 subtract. Multiplying If we multiply the fractions three tenths and seven tenths, the decimal product is twenty-one hundredths. numbers $\frac{3}{10} \times \frac{7}{10} = \frac{21}{100}$ Likewise, if we multiply the decimal numbers three tenths and seven tenths, the product is twenty-one hundredths. $0.3 \times 0.7 = 0.21$ Here we use an area model to illustrate this multiplication: 0.3 0.7Each side of the square is one unit in length. We multiply three tenths of one side by seven tenths of a perpendicular

Math 8/7, Lesson 35 Sample taken from Math 8/7 (Third Edition), page 237

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	side. The product is an area that contains twenty-one hundredths of the square.
	$0.3 \times 0.7 = 0.21$
	Notice that the factors each have one decimal place and the product has two decimal places. When we multiply decimal numbers, the product has as many decimal places as there are in all the factors combined.
Example 5	Multiply: (0.23)(0.4)
Solution	We need not align decimal points to multiply. We set up the problem as though we were multiplying whole numbers. After multiplying, we count the number of decimal places in both factors. There are a total of three decimal places, so we write the product with three decimal places. We count from right to left, writing one or more zeros in front as necessary. The product of 0.23 and 0.4 is 0.092.
Example 6	Multiply: 35 × 0.4
Solution	We set up the problem as though we were multiplying whole numbers. After multiplying, we count the total number of decimal places in the factors. Then we place a decimal point in the product so that the product has the same number of decimal places as there are in the factors combined. After placing the decimal point, we simplify the result. $\begin{array}{ll} 35 & 0 \text{ places} \\ \times & 0.4 & 1 \text{ place} \\ 14.0 & 1 \text{ place} \end{array}$
Example 7	Multiply: (0.2)(0.3)(0.04)
Solution	Sometimes we can perform the multiplication mentally. First we multiply as though we were multiplying whole numbers: $2 \cdot 3 \cdot 4 = 24$. Then we count decimal places. There are four decimal places in the three factors. Starting from the right side of 24, we count to the left four places. We write zeros in the empty places.
	·∞24 → 0.0024

Math 8/7, Lesson 35 Sample taken from Math 8/7 (Third Edition), page 238

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Dividing decimal numbers	Dividing a decimal number by a whole number is similar to dividing money. The decimal point in the answer is straight up from the decimal point in the division box.
Example 8	Divide: 3.425 ÷ 5
Solution	We rewrite the problem with a division 0.685 box. We place a decimal point in the $5)3.425$ answer directly above the decimal $3 0$ point in the division box. Then we 42 divide as though we were dividing 40 whole numbers. The answer is 0.685 . 25 25 0
Example 9	Divide: 0.0144 ÷ 8
Solution	We place the decimal point in the answer directly above the decimal point inside the division box. We write a digit in every place following the decimal point until the division is completed. If we cannot perform a division, we write a zero in that place. 0.0018 8 We place the decimal 64 0.00144 0.00144 0.00144 0.00144 0.00144 0.00144 0.0018
Example 10	Divide: 1.2 ÷ 5
Solution	We do not write a decimal division answer with a remainder. Since a decimal point fixes place values, we may write a zero in the next decimal place. This zero does not change the value of the number, but it does let us continue dividing. The answer is 0.240.24 0 10 20 0
LESSON PRACT	ICE
Practice set*	Simplify: a. 1.2 + 3.45 + 23.6 b. 4.5 + 0.51 + 6 + 12.4
	c. $0.2 + 0.4 + 0.6 + 0.8$ d. $36.274 - 5.39$
	e. 16.7 - 1.936 f. 12 - 0.875

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	-	Lesson 35 239
g.	4.2×0.24	h. (0.12)(0.06)
i.	5.4×7	j. 0.3 \times 0.2 \times 0.1
k.	(0.04)(10)	l. 0.045 × 0.6
m.	$14.4 \div 6$	n. 0.048 ÷ 8
0.	$3.4 \div 5$	p. 0.3 ÷ 6
MIXED PRACTICE		
Problem set 1.	During the first six months monthly electric bills were \$96.25, \$81.70, and \$71.70 find their average monthly months of the year?	of the year, the Montgomerys' e \$128.45, \$131.50, \$112.30, . How can the Montgomerys electric bill for the first six
2. (23, 30)	There were $2\frac{1}{2}$ gallons of m breakfast. There were $1\frac{3}{4}$ gal gallons of milk were consum	nilk in the refrigerator before llons after dinner. How many ned during the day?
3. (20)	A one-year subscription to \$15.60. The regular newsst How much is saved per issu price?	a monthly magazine costs and price is \$1.75 per issue. are by paying the subscription
4. (24)	Carlos ran one lap in 1 minu lap 5 seconds faster than Car take Orlando to run one lap?	te 3 seconds. Orlando ran one los. How many seconds did it
5. (19)	The perimeter of the square the perimeter of the pentagon. Each side of pentagon is 16 cm long. Ho is each side of the square?	e equals regular of the ow long
6. (22)	Diagram this statement. That follow.	Then answer the questions
	Two ninths of the 54 guppies.	fish in the tank were
	(a) How many of the fish w	ere guppies?
×.	(b) How many of the fish w	ere not guppies?







Sample taken from Math 8/7 (Third Edition), page 446

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Because we know both total numbers, we will also use the "total" row. Using these numbers, we solve the proportion.

[Ratio	Actual Count	1			
Boys	5	B	1			
Girls	4	G		4		G
Total	9	180		9	=	180
			Q	G	=	720
				G	=	80

We find there were 80 girls at the concert. We can use this answer to complete the ratio box.

	Ratio	Actual Count
Boys	5	100
Girls	4	80
Total	9	180

Example The ratio of football players to soccer players in the room was 5 to 7. If the football and soccer players in the room totaled 48, how many were football players?

Solution We use the information in the problem to form a table. We include a row for the total number of players. The total ratio number is 12.



To find the number of football players, we write a proportion from the "football players" row and the "total players" row. We solve the proportion to find that there were 20 football players in the room. From this information we can complete the ratio box.

	Ratio	Actual Count	
Football players	5	20	
Soccer players	7	28	
Total players	12	48	

LESSON PRACT	Lesson 65 44
Practice set	Solve these problems. Begin by drawing a ratio box. a. Acrobats and clowns converged on the center ring in th ratio of 3 to 5. If a total of 72 acrobats and clowns performe in the center ring, how many were clowns?
	b. The ratio of young men to young women at the ball was to 9. If 240 young men were in attendance, how man young people attended in all?
MIXED PRACTI	CE
Problem set	 If 5 pounds of apples cost \$2.40, then (a) what is the price per pound? (b) what is the cost for 8 pounds of apples?
	 (a) Simplify and compare: (0.3)(0.4) + (0.3)(0.5) ○ 0.3(0.4 + 0.5) (b) What property is illustrated by this comparison?
	3. Use a ratio box to solve this problem. The ratio of big fis to little fish in the pond was 4 to 11. If there were 1320 fis in the pond, how many big fish were there?
	 The car traveled 350 miles on 15 gallons of gasoline. Th car averaged how many miles per gallon? Round th answer to the nearest tenth.
	5. The average of 2 and 4 is 3. What is the average of th $^{\scriptscriptstyle (2M)}$ reciprocals of 2 and 4?
	6. Write 12 billion in scientific notation.
	 Diagram this statement. Then answer the question (22, 30) that follow.
	One sixth of the five dozen eggs were cracked.
	(a) How many eggs were not cracked?
	(b) What was the ratio of eggs that were cracked to egg that were not cracked?
	(c) What percent of the eggs were cracked?





450 Saxon Math 8/7—Homeschool 22. Answer true or false: (a) All equilateral triangles are congruent. (b) All equilateral triangles are similar. 23. The bar was raised from 2.15 meters to 2.2 meters. How (32.34) many centimeters was the bar raised? Simplify: 24. $\frac{10^3 \cdot 10^3}{10^2}$ 25. 4 days 5 hr 15 min (66) - 1 days 7 hr 50 min 26. $4.5 \div (0.4 + 0.5)$ 27. $\frac{3 + 0.6}{3 - 0.6}$ 28. $4\frac{1}{5} \div (1\frac{1}{6} \cdot 3)$ 29. $3^2 + \sqrt{4 \cdot 7 - 3}$ 30. |-3| + 4[(5 - 2)(3 + 1)]



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steep. The "slant" of the graph of a function is called its slope. We assign a number to a slope to indicate how steep the slope is and whether the slope is upward or downward. If the slope is upward, the number is positive. If the slope is downward, the number is negative. If the graph is horizontal, the slope is neither positive nor negative; it is zero. If the graph is vertical, the slope cannot be determined.

Example 1 State whether the slope of each line is positive, negative, zero, or cannot be determined.



Solution

To determine the sign of the slope, follow the graph of the function with your eyes from left to right as though you were reading.

- (a) From left to right, the graphed line rises, so the slope is positive.
- (b) From left to right, the graphed line does not rise or fall, so the slope is zero.
- (c) From left to right, the graphed line slopes downward, so the slope is negative.
- (d) There is no left to right component of the graphed line, so we cannot determine if the line is rising or falling. The slope is not positive, not negative, and not zero. The slope of a vertical line cannot be determined.

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To determine the numerical value of the slope of a line, it is helpful to draw a right triangle using the background grid of the coordinate plane and a portion of the graphed line. First we look for points where the graphed line crosses intersections of the grid. We have circled some of these points on the graphs below.



Next we select two points from the graphed line and, following the background grid, sketch the legs of a right triangle so that the legs intersect the chosen points. (It is a helpful practice to first select the point to the left and draw the horizontal leg to the right. Then draw the vertical leg.)



We use the words **run** and **rise** to describe the two legs of the right triangle. The *run* is the length of the horizontal leg, and the *rise* is the length of the vertical leg. We assign a positive sign to the rise if it goes up to meet the graphed line and a negative sign if it goes down to meet the graphed line. In the graph on the left, the run is 2 and the rise is +3. In the graph

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on the right, the run is 2 and the rise is -1. We use these numbers to write the slope of each graphed line.

So the slopes of the graphed lines are these ratios:

 $\frac{\text{rise}}{\text{run}} = \frac{+3}{2} = \frac{3}{2}$ $\frac{\text{rise}}{\text{run}} = \frac{-1}{2} = -\frac{1}{2}$

The slope of a line is the ratio of its rise to its run ("rise over run").

 $slope = \frac{rise}{run}$

A line whose rise and run have equal values has a slope of 1. A line whose rise has the opposite value of its run has a slope of -1.



A line that is steeper than the lines above has a slope either greater than 1 or less than -1. A line that is less steep than the lines above has a slope that is between -1 and 1.





Sample taken from Math 8/7 (Third Edition), page 746

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Solution We note that the slope is positive. We locate and select two points where the graphed line passes through intersections of the grid. We choose the points (0, -1) and (3, 1). Starting from the point to the left, (0, -1), we draw the horizontal leg to the right. Then we draw the vertical leg up to (3, 1).



We see that the run is 3 and the rise is positive 2. We write the slope as "rise over run."

Slope =
$$\frac{2}{3}$$

Note that we could have chosen the points (-3, -3) and (3, 1). Had we done so, the run would be 6 and the rise 4. However, the slope would be the same because $\frac{4}{6}$ reduces to $\frac{2}{3}$.

One way to check the calculation of a slope is to "zoom in" on the graph. When the horizontal change is one unit to the right, the vertical change will equal the slope. To illustrate this, we will zoom in on the square just below and to the right of the origin on this graph. This method is a check for reasonableness of calculated slopes and can help prevent mistakes such as inverted slopes.





Math 8/7, Lesson 107 Sample taken from Math 8/7 (Third Edition), page 748

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MIXED PRACTI	CE
Problem set	1. The shirt regularly priced at \$21 was on sale for $\frac{1}{3}$ off. What was the sale price?
	2. Nine hundred seventy-five billion is how much less than ⁽⁵¹⁾ one trillion? Write the answer in scientific notation.
	3. What is the (a) range and (b) mode of this set of numbers?
	16, 6, 8, 17, 14, 16, 12
	Use ratio boxes to solve problems 4–6.
	4. Riding her bike from home to the lake, Sonia averaged ⁽⁷²⁾ 18 miles per hour (per 60 minutes). If it took her 40 minutes to reach the lake, how far did she ride?
	5. The ratio of earthworms to cutworms in the garden was 5 to 2. If there were 140 earthworms and cutworms in the garden, how many were earthworms?
	6. The average cost of a new car increased 8 percent in one (92) year. Before the increase the average cost of a new car was \$16,550. What was the average cost of a new car after the increase?
	7. The points (3, -2), (-3, -2), and (-3, 6) are the vertices of ⁽⁸⁸⁾ a right triangle. Find the perimeter of the triangle.
	8. In this figure, $\angle ABC$ is a right angle. (a) Find m $\angle ABD$. (b) Find m $\angle DBC$. (c) $A^{DD}C$. (c) $A^{DD}C$
	(c) Find m∠BCD.
	(d) Which triangles in this figure are similar?
	Write equations to solve problems 9–11.
	9. Sixty is 125 percent of what number?
	10. Sixty is what percent of 25?



- 11. Sixty is four more than twice what number?
- In a can are 100 marbles: 10 yellow, 20 red, 30 green, and (84, INV. 10) 40 blue.
 - (a) If a marble is drawn from the can, what is the chance that the marble will not be red?
 - (b) If the first marble is not replaced and a second marble is drawn from the can, what is the probability that both marbles will be yellow?

13. Complete the table.

FRACTION	DECIMAL	PERCENT
<u>5</u> 6	(a)	(b)

14. Compare: $(x - y)^2 \bigcirc (y - x)^2$ if x > y

Multiply. Write the product in scientific notation.

 $(1.8 \times 10^{10})(9 \times 10^{-6})$

16. (a) Between which two consecutive whole numbers is $\sqrt{600?}$

- (b) What are the two square roots of 10?
- 17. Find three x, y pairs for the function y = x + 1.
 - (a) Graph these number pairs on a coordinate plane and draw a line through the points.

(b) What is the slope of the graphed line?

 If the radius of this circle is 6 cm, (104) what is the area of the shaded region?



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 Find the surface area of this rectangular solid. Dimensions are in inches.



Math 8/7, Investigation 5



Math 8/7, Investigation 5



Math 8/7, Investigation 5

Sample taken from Math 8/7 (Third Edition), page 348



We see that the sector labeled "food" is 20% of the area of the circle, representing 20% of the income. To make a 20% sector, we could draw a central angle that measures 20% of 360°.

20% of 360°

$0.2 \times 360^{\circ} = 72^{\circ}$

With a protractor we can draw a central angle of 72° to make a sector that is 20% of a circle.

Math 8/7, Investigation 5 Sample taken from Math 8/7 (Third Edition), page 349

				Investigation 5	349
				West	
	 Create a pie graph for spends a weekday. I in the central angle use a compass to dr inches. Then, with the circle into sector sector. 	or the tabl First calcu for each s aw a circl a protract ors of the	e below ilate the ector of e with a or and s correct s	to show how number of de the pie graph. radius of abo traightedge, d size and label	Kerry egrees Next out 2 ¹ / ₂ livide each
	,	How Kerry Spr	ends a Day		
		Activity	% of Day	1	
		Studies	25%	1	
		Recreation	10%	1	
	1	Music lessons	10%	1	
		Eating	10%	1	
		Sleeping	40%		
		Other	5%	19	
Extensions	 a. Create a circle grap friends and family w b. Explore the graph computer programs. 	oh showir vith variou n-creating	ig the p is eye co capabil	ercentages of lors. lities of dat	your abase

